Continuous dependence of solutions on a parameter of abstract generalized linear differential equations (Opial type results)

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In this work we continue our research from [1] on continuous dependence on a parameter k of solutions to linear integral equations of the form

$$x(t) = \tilde{x}_k + \int_a^t d[A_k] x + f_k(t) - f_k(a), \quad t \in [a, b], k \in \mathbb{N}, \qquad (eq_k)$$

where $A_k: [a, b] \to L(X)$ have bounded variations on $[a, b], f_k: [a, b] \to X$ are regulated on [a, b] and $\tilde{x}_k \in X$, with X being a Banach space. The integrals are understood as the abstract Kurzweil-Stieltjes integrals and the studied equations are usually called generalized linear differential equations (in the sense of J. Kurzweil)

Focusing our attention on the case when the variations $\operatorname{var}_a^b A_k$ need not be uniformly bounded, we extend Theorem 4.2 from [1], which is an analogy of the classical Opial's result for ODEs. Finally, we provide an example showing that the obtained conditions are somehow optimal.

This talk is based on a joint work with Milan Tvrdý.

References

- MONTEIRO G.A. AND TVRDÝ M.: Generalized linear differential equations in a Banach space: Continuous dependence on a parameter. Discrete Contin. Dyn. Syst. 33 (1) (2013), 283–303, doi:10.3934/dcds.2013.33.283.
- [2] MONTEIRO G.A. AND TVRDÝ M.: Continuous dependence of solutions of abstract generalized linear differential equations with potential converging uniformly with a weight. submitted