On the initial value problem for functional-differential equations

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We consider the initial value problem for a linear functional differential system of the general form

$$
\begin{aligned}
&u_k'(t) = (l_k u)(t) + q_k(t), \qquad t \in [a,b],\ k = 1,2,\ldots,n,\\
&u_k(\tau) = c_k, \qquad k = 1,2,\ldots,n,
\end{aligned}
$$

where $-\infty < a \le \tau \le b < \infty$, $n \in \mathbb{N}$, $l = (l_k)_{k=1}^n : C([a,b],\mathbb{R}^n) \to L_1([a,b],\mathbb{R}^n)$ is an arbitrary bounded linear mapping, $\{c_1, c_2, \ldots, c_n\} \subset \mathbb{R}$, and $q = (q_k)_{k=1}^n : [a,b] \to \mathbb{R}^n$ are Lebesgue integrable functions. Some new and, in a sense, optimal constructive unique solvability conditions are obtained. The question on the monotonous dependence of the solution on the forcing terms and some generalisations are also discussed.