Non-ordered periodic upper and lower solutions for difference equation with discret ϕ -Laplacian

Cristian Bereanu

Louvain-la-Neuve, Belgium

Let $\phi : \mathbb{R} \to] - a, a[(0 < a \le \infty)$ be an increasing homeomorphism with $\phi(0) = 0$. Let also $n \ge 3$ be an integer and $f_m : \mathbb{R} \to \mathbb{R} \ (2 \le m \le n-1)$ be continuous functions. Assume that the periodic boundary value problem

 $D\phi(Dx_m) + f_m(x_m, Dx_m) = 0$ $(2 \le m \le n-1), \quad x_1 = x_n, \quad Dx_1 = Dx_{n-1}$

has a lower solution α and an upper solution β . If f_m $(2 \le m \le n-1)$ are bounded from below (with bounds sufficiently small when ϕ is bounded), then we prove that we have existence.

This result is a joint work with Jean Mawhin and is a discrete version of a result due to Irena Rachůnková and Milan Tvrdý.