Non-negative periodic solutions to second-order differential equations with sublinear nonlinearities

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We will present efficient conditions for the existence and uniqueness of a non-trivial non-negative ω -periodic solution to the equation

$$u'' = p(t)u + q(t, u) \tag{1}$$

with a sublinear nonlinearity q. A particular case of (1) will be discussed in detail, namely,

$$u'' = p(t)u + h(t)|u|^{\lambda}\operatorname{sgn} u,$$
(2)

where $\lambda \in [0, 1[$. The results obtained will be compared with the facts which can be derived for equation (2) in the autonomous case, i. e., if the coefficients *p* and *h* are constants.